



Dense and Narrow Reflection-Bands Structure Based on One Dimensional Photonic Crystal

Satyendra Pratap Singh¹, Dipanjan De²
M.Tech Student¹, HOD²

Department of Electronics and Communication
United Institute of Technology, Naini, Allahabad, U.P, India

Abstract:

In this paper filters designed with normal incident of light that produced dense reflection bands with narrow band gap. Filters made of one dimensional Photonic crystal composed of three layers of Silicon Dioxide, Titanium Dioxide and Air. Thickness of layers specified to result in small total thickness of filter. Four filters got proposed with three layers that differ in layers arrangements and layer thickness. After specific repetition of periods showed nearly no effect on reflection bands when number of periods are increased at wavelength near 1550nm. Filters produced minimum quality factor of 7048 and reflection band gap near 0.22nm. Gap between two stop bands is nearly 0.45nm for all filters. All calculations are done with the help of Transfer Matrix Method in Mat-Lab.

Keywords: Total thickness, Transfer Matrix Method, Dense reflection bands, Narrow bands, Quality factor, Band gap, Photonic Crystals.

I. INTRODUCTION:

Now days research on Photonic crystal is increasing for making optical communication more advance and compressing the size of each devices of communication system. New generation services with high speed internet growth cause a large traffic in communication. DWDM system can full fill need of more bandwidth for networks by its more number of channels with narrower channel spacing. Optical filter is a device for selectively transmitting or reflecting light in particular range of wavelengths while the other blocked. Band structure produced by photonic crystals have special regions where no optical waves are allowed to propagate (reflected back) are known as Photonic band gaps (PBG). These filters are also separating (Demultiplex) one optical channel from combined signals. So need to stop some channels lead the requirement of stop band filters. Its widespread uses are found in various areas of interest such as nanotechnology, astronomy and communication. Designing is the first step in making an effective channel filter in many applications. In this paper filters with 20 periods, each period compose of three layers. Paper considers normal incident of optics and effects on reflection bands only. Number of reflection bands got increased by selecting specific thickness of third layer (air) of each period. Three layers are Silicon dioxide, Titanium dioxide and Air. Third player selected as Air to have minimum total loss in photonic crystal. Paper is divided in two parts as per change in thickness of third layer (Air) in each period. Rest of two layers has constant thickness. First part where thickness of Air is large having two types of filter with period designed as ABC and ACB. Symbols A, B and C represent SiO₂, TiO₂ and Air respectively. Similarly, in second part where thickness of Air is small having two types of filter with period designed as ABC and ACB. All four filters producing dense and narrow reflection bands, so these features make it applicable for optical communication, optical wave guide, optical reflector, de-

multiplexer etc. Range of wavelength where all filters can produce better result is 1300-1700(nm). Refractive indexes are 1.46, 2.4 and 1 of SiO₂, TiO₂ and air respectively [3]. Paper depicted sample of result only for wavelength range of 1550nm to 1555nm producing 7 reflection bands. Band gap of reflection band comes out nearly 0.22nm. Gap between two stop bands is nearly 0.45nm. Quality factors are near 7048. All four filters are showing nearly no effect on reflection bands when number of periods are increasing after nearly N=20 (e.g. N=30, N=40 and N=50 etc.). Results are same for TE and TM mode when work on normal incident angle to filter and recorded all results. All calculations are done with the help of Transfer Matrix Method on Mat-Lab by simulations.

Structure of filter:



Figure. 1 One period made of three layers

Note: This period is repeated for 20 times in every filter in paper. This period is made of three materials with different thickness.

Theory:

n_1 =refractive index of SiO₂

n_2 =refractive index of TiO_2
 n_3 =refractive index of Air

Thickness of layers are taken as follow

h_1 =thickness of SiO_2
 h_2 =thickness of TiO_2
 h_3 =thickness of Air

Let denote these three layers with following symbols

- A. - layer with n_1 and h_1
- B. - layer with n_2 and h_2
- C. - layer with n_3 and h_3

Dynamic Matrix for each layers are given by:

$$D_m = \begin{cases} \begin{bmatrix} 1 & 1 \\ n_m \cos \Theta_m & -n_m \cos \Theta_m \end{bmatrix} TE \text{ mode} \\ \begin{bmatrix} \cos \Theta_m & \cos \Theta_m \\ n_m & -n_m \end{bmatrix} TM \text{ mode} \end{cases}$$

$m=1, 2, 3.$

Where n_m is refractive index of m^{th} layer
 And Θ_m is incident angle to m^{th} layer

And Dynamic Matrix for Air is given by:

$$D_0 = \begin{cases} \begin{bmatrix} 1 & 1 \\ n_0 \cos \Theta_0 & -n_0 \cos \Theta_0 \end{bmatrix} TE \text{ mode} \\ \begin{bmatrix} \cos \Theta_0 & \cos \Theta_0 \\ n_0 & -n_0 \end{bmatrix} TM \text{ mode} \end{cases}$$

Where n_0 is refractive index of Air
 And Θ_0 is incident angle to layer

And propagation Matrix for each layer is given by:

$$P_m = \begin{bmatrix} e^{(ik_m h_m)} & 0 \\ 0 & e^{(-ik_m h_m)} \end{bmatrix}$$

$m=1, 2$

Where each layer has its own wave vector
 $k_m = 2\pi n_m \cos \Theta_m / \lambda$

Transfer matrix for each period made of three layers is given by:

$$M_p = D_1 P_1 D_1^{-1} D_2 P_2 D_2^{-1} D_3 P_3 D_3^{-1}$$

Total Transfer Matrix of total structure with period 20 is given by:

$$M = D_0^{-1} M_p^{20} D_0 = \begin{bmatrix} M_{11} & M_{12} \\ M_{21} & M_{22} \end{bmatrix}$$

Where D_0 is dynamic matrix of air that surrounds total structure Reflection coefficient is given by:

$$r = \frac{M_{21}}{M_{11}}$$

Reflectance is given by:

$$R = |r|^2$$

And, Transmission coefficient is given by:

$$t = \frac{1}{M_{11}}$$

Transmittance is given by:

$$T = |t|^2$$

Expressions and methods are taken from reference papers [1-21].

Calculation with results:

Following 'Four filters' are proposed:

1. First part:

a. First filter:

Filter with period 'ABC' have following specifications of layers:

Refractive indexes are $n_1=1.46, n_2=2.4, n_3=1.$

Thicknesses are critically given in nm for more accuracy as $h_1=410958.9041, h_2=250000, h_3=600388.3497,$ but value can be approximated.

Output table is given below:

Table no. 1			
Band no.	λ_0 (nm)	$\Delta\lambda$ (nm)	Quality factor(Q)
1	1550.72	0.22	7048.7
2	1551.39	0.22	7051.8
3	1552.06	0.22	7054.8
4	1552.73	0.22	7057.9
5	1553.40	0.22	7060.9
6	1554.07	0.22	7064
7	1554.74	0.22	7067

First filter period ABC TE mode N=20

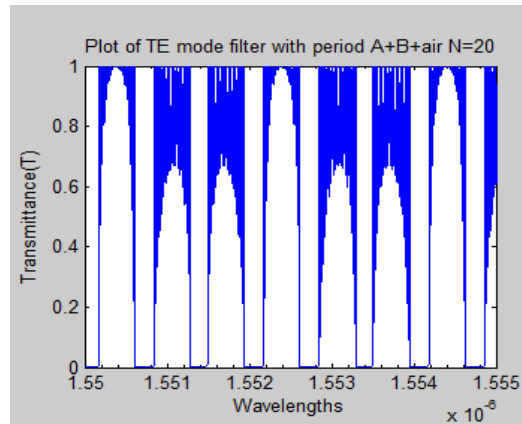


Figure.2. Plot of reflection bands of filter with period 'ABC' for TE mode with N=20

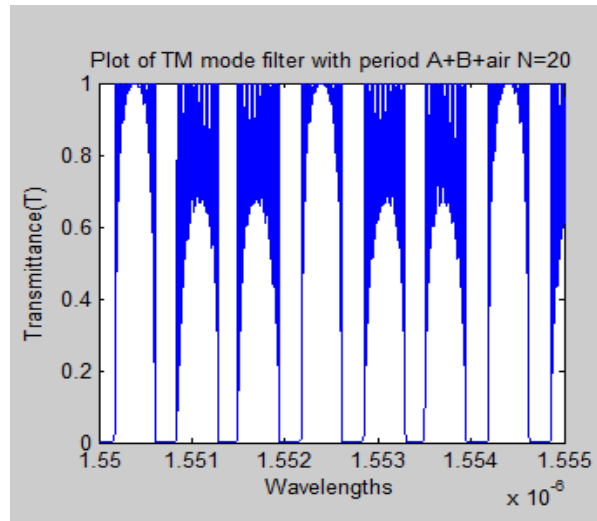


Figure.3. Plot of reflection bands of filter with period 'ABC' for TM mode with N=20

Both TE and TM modes are producing same reflection bands for normal incident. Total 7 bands are there in range of 1550nm to 1555nm of wavelengths. Each band having nearly 0.22nm reflection bands gap. Gap between two stop bands is nearly 0.45nm. Minimum Quality factor is near 7048. In following figures as no. of periods increase with N=30, N=40 and N=50

for TE mode showing nearly no effect on structure of reflection bands

Output table is given below:

Table no. 2			
Band no.	λ_0 (nm)	$\Delta\lambda$ (nm)	Quality factor(Q)
1	1550.72	0.22	7048.7
2	1551.39	0.22	7051.8
3	1552.06	0.22	7054.8
4	1552.73	0.22	7057.9
5	1553.40	0.22	7060.9
6	1554.07	0.22	7064
7	1554.74	0.22	7067

Second filter period ACB TE mode N=20

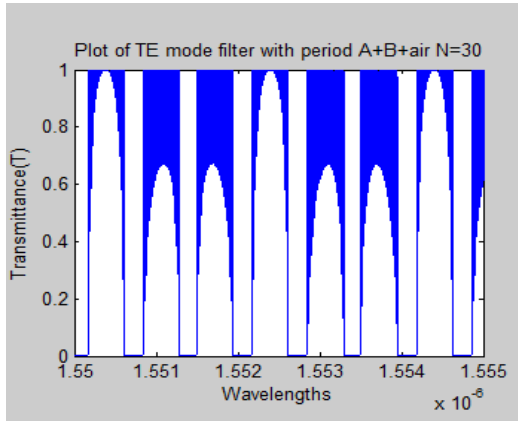


Figure.4. Plot of reflection bands of filter with period 'ABC' for TE mode with N=30

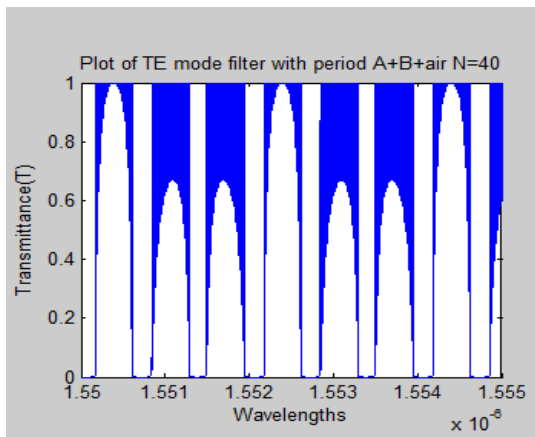


Figure.5. Plot of reflection bands of filter with period 'ABC' for TE mode with N=40

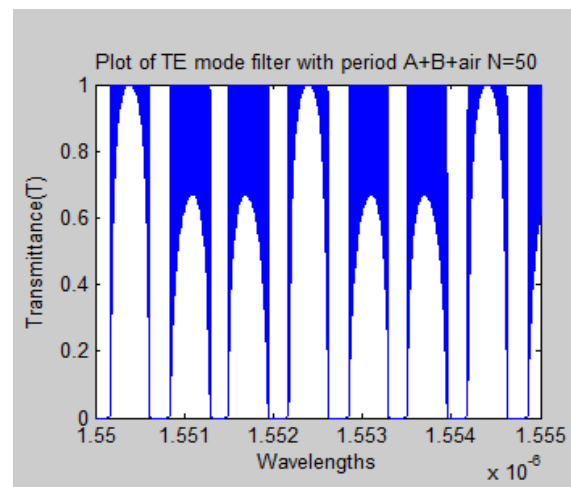


Figure.6. Plot of reflection bands of filter with period 'ABC' for TE mode with N=50

b. Second filter:

Filter with period 'ACB' have following specifications of layers as:

Refractive indexes are $n_1=1.46$, $n_2=2.4$ and $n_3=1$. Thicknesses are critically given in nm for more accuracy as $h_1=410958.9041$, $h_2=250000$ and $h_3=600388.3497$, but value can be approximated.

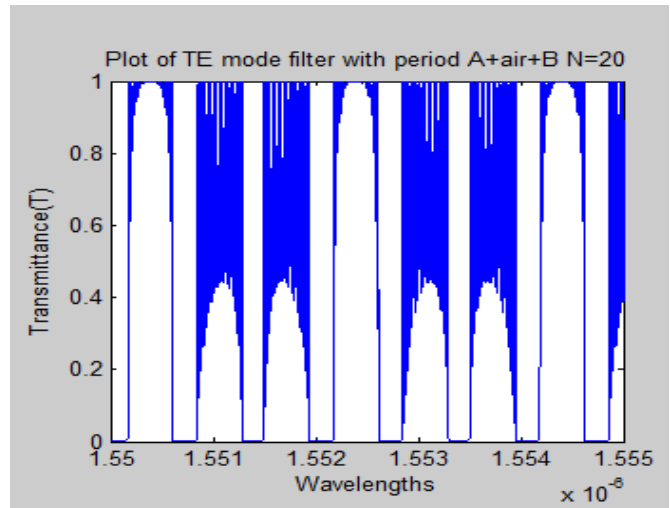


Figure.7. Plot of reflection bands of filter with period 'ACB' for TE mode with N=20

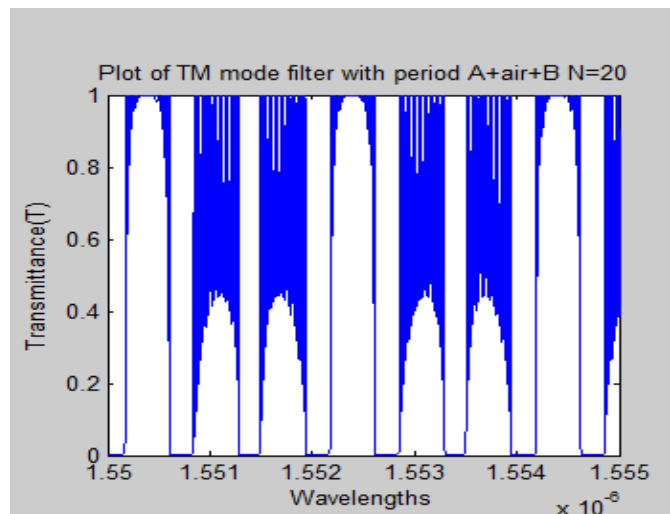


Figure.8. Plot of reflection bands of filter with period 'ACB' for TM mode with N=20

Both TE and TM modes are producing same reflection bands for normal incident. Total 7 bands are there in range of 1550nm to 1555nm of wavelengths. Each band having nearly 0.22nm reflection bands gap. Gap between two stop bands is nearly 0.45nm. Minimum quality factor is near 7048. In following figures as no. of periods increase with N=30, N=40 and N=50

for TE mode showing nearly no effect on structure of reflection bands.

Output table is given below:

Table no. 3			
Band no.	λ_0 (nm)	$\Delta\lambda$ (nm)	Quality factor(Q)
1	1550.72	0.22	7048.7
2	1551.39	0.22	7051.8
3	1552.06	0.22	7054.8
4	1552.73	0.22	7057.9
5	1553.40	0.22	7060.9
6	1554.07	0.22	7064
7	1554.74	0.22	7067

Third filter period ABC TE mode N=20

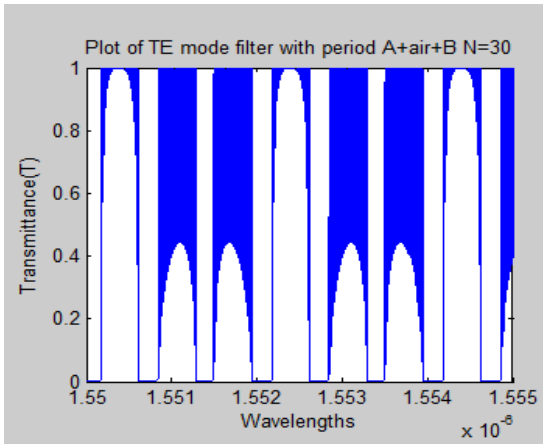


Figure.9. Plot of reflection bands of filter with period ‘ACB’ for TE mode with N=30

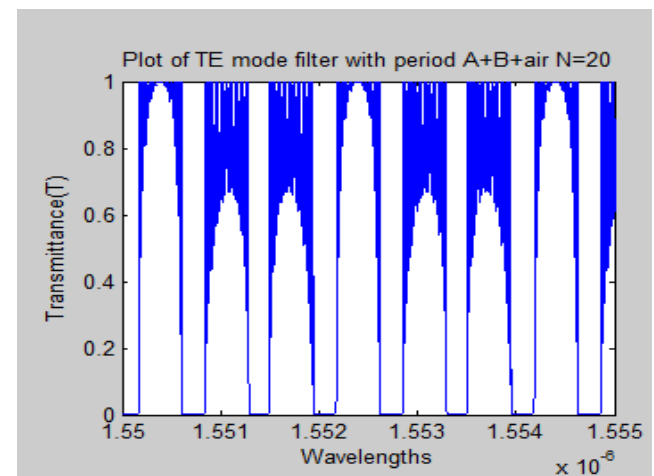


Figure.12. Plot of reflection bands of filter with period ‘ABC’ for TE mode with N=20

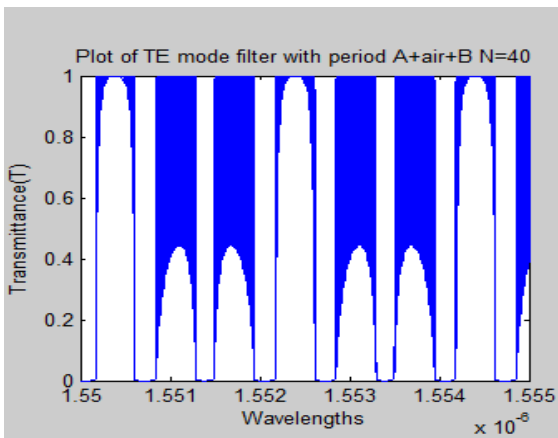


Figure.10. Plot of reflection bands of filter with period ‘ACB’ for TE mode with N=40

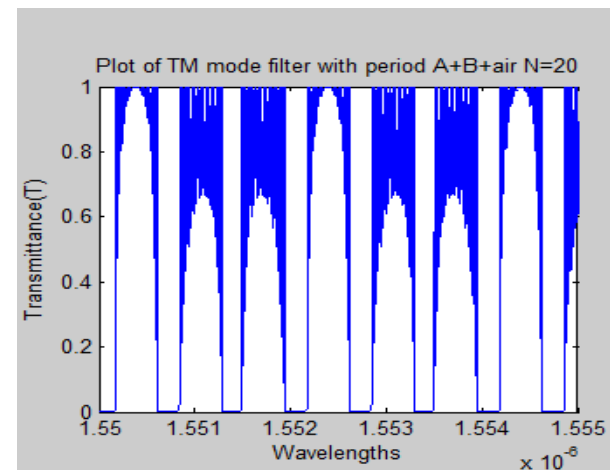


Figure.13. Plot of reflection bands of filter with period ‘ABC’ for TM mode with N=20

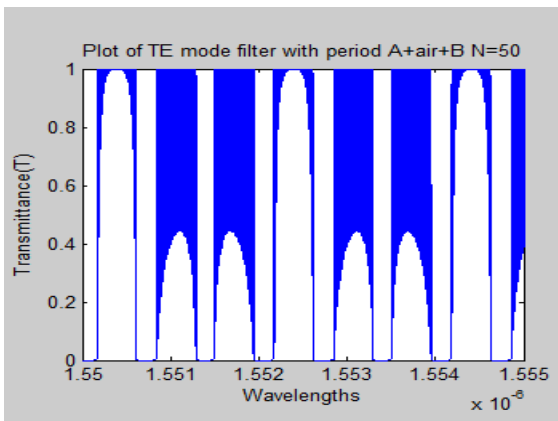


Figure.11. Plot of reflection bands of filter with period ‘ACB’ for TE mode with N=50

2. Second part:

a) Third filter:

Filter with period ‘ABC’ have following specifications of layers as:

Refractive indexes are $n_1=1.46$, $n_2=2.4$ and $n_3=1$. Thicknesses are critically given in nm for more accuracy as $h_1=410958.9041$, $h_2=250000$ and $h_3=599612.1528$, but value can be approximated.

Both TE and TM modes are producing same reflection bands for normal incident. Total 7 bands are there in range of 1550nm to 1555nm of wavelengths. Each band having nearly 0.22nm reflection bands gap. Gap between two stop bands is nearly 0.45nm. Minimum quality factor is near 7048. In following figures as no. of periods increase with N=30, N=40 and N=50

TE mode showing nearly no effect on structure of reflection bands.

$h_1=410958.9041$, $h_2=250000$ and $h_3=599612.1528$, but value can be approximated.

Output table is given below as:

Table no. 4			
Band no.	λ_0 (nm)	$\Delta\lambda$ (nm)	Quality factor(Q)
1	1550.72	0.22	7048.7
2	1551.39	0.22	7051.8
3	1552.06	0.22	7054.8
4	1552.73	0.22	7057.9
5	1553.40	0.22	7060.9
6	1554.07	0.22	7064
7	1554.74	0.22	7067

Fourth filter period ACB TE mode N=20

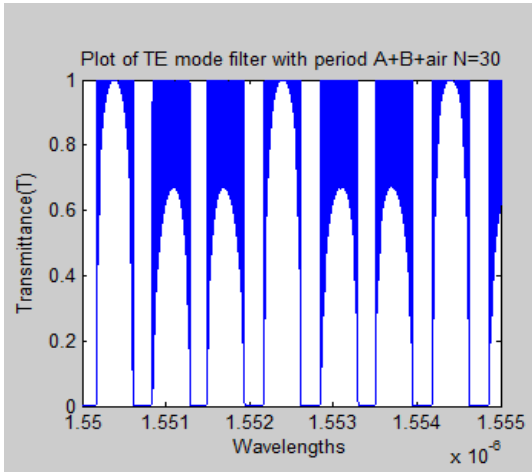


Figure.14. Plot of reflection bands of filter with period 'ABC' for TE mode with N=30

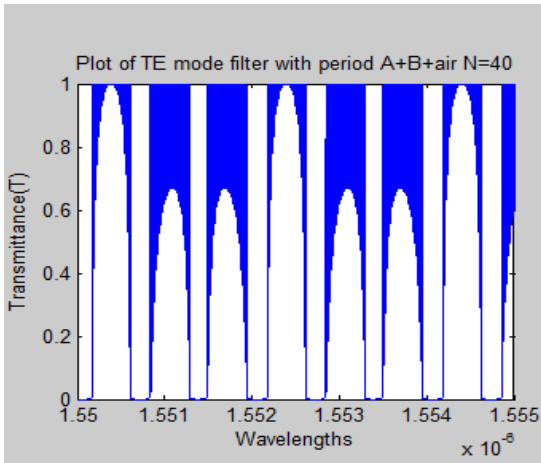


Figure.15. Plot of reflection bands of filter with period 'ABC' for TE mode with N=40

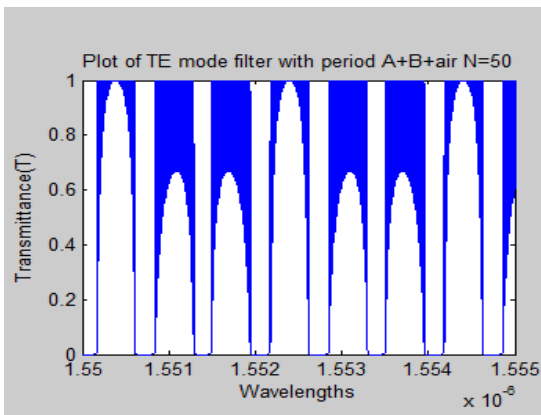


Figure.16. Plot of reflection bands of filter with period 'ABC' for TE mode with N=50

c. Fourth filter:

Filter with period 'ACB' have following specifications of layers as:
 Refractive indexes of layers are $n_1=1.46$, $n_2=2.4$ and $n_3=1$.
 Thicknesses are critically given in nm for more accuracy as

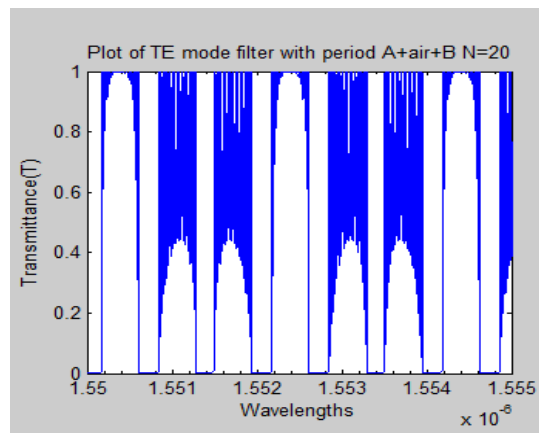


Figure.17. Plot of reflection bands of filter with period 'ACB' for TE mode with N=20

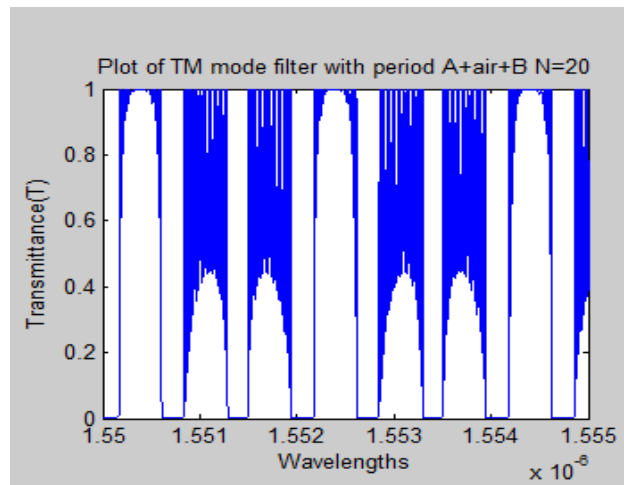


Figure.18. Plot of reflection bands of filter with period 'ACB' for TM mode with N=20

Both TE and TM modes are producing same reflection bands for normal incident. Total 7 bands are there in range of 1550nm to 1555nm of wavelengths. Each band having nearly 0.22nm reflection bands gap. Gap between two stop bands is nearly 0.45nm. Minimum quality factor is near 7048. In following figures as no. of periods increase with N=30, N=40 and N=50

for TE mode showing nearly no effect on structure of reflection bands.

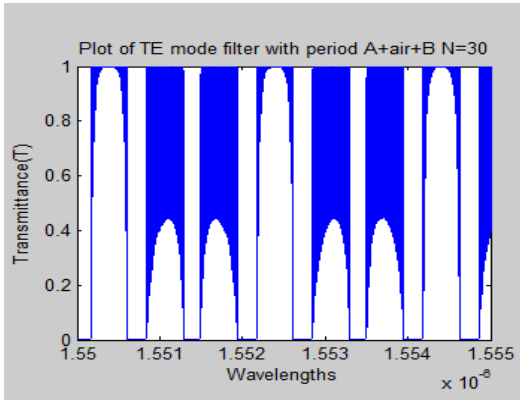


Figure.19. Plot of reflection bands of filter with period 'ACB' for TE mode with N=30

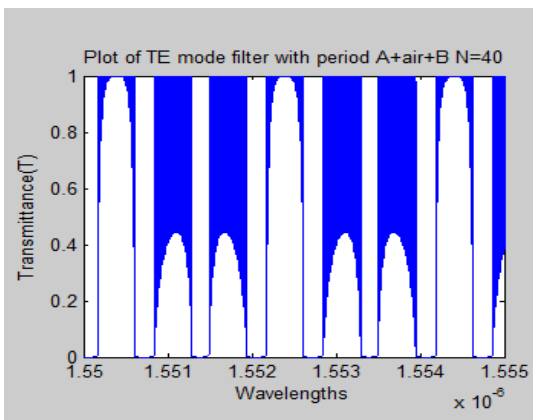


Figure.20. Plot of reflection bands of filter with period 'ACB' for TE mode with N=40

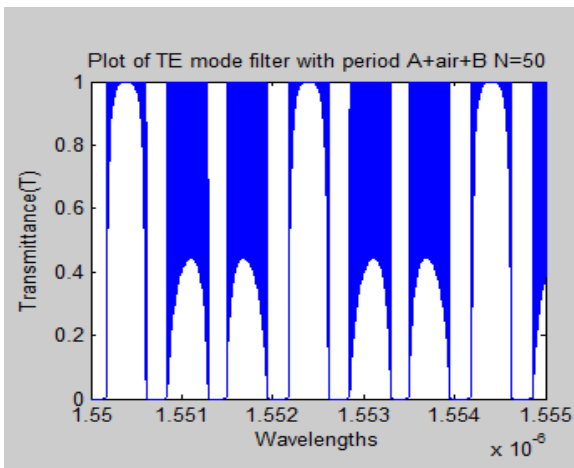


Figure.21. Plot of reflection bands of filter with period 'ACB' for TE mode with N=50

II. CONCLUSION:

In this paper we designed four filters each with period of three layers as Silicon dioxide, Titanium dioxide and Air. Paper considered normal incident of light and effect on reflection bands only. Due to consideration of layer of air total loss in filter reduced. Each of layers considered with a specific thickness so that we got success in minimizing total thickness of filter.

Outputs of all four filters are producing dense and narrow reflection bands. This made more applicable in optical communication system, where DWDM schemes are running. These filters are also got application optical waveguide, optical reflector, optical de-multiplexer etc. All filters are producing quality factor near 7048 and reflection band gap is near 0.22nm. Gap between two stop bands is nearly 0.45nm for all filters. There are 7 bands in ranges of 1550nm to 1555nm.

III. REFERENCES:

- [1]. Farhad Mehdizadeh , Hamed ,Alipour, Banaei, Ziaddin Daie, Kuzekanani, All Optical Multi Reflection Structure Based On One Dimensional Photonic Crystals For WDM Communication Systems, *Optoelectronics and Advanced Materials, Rapid communication*, ,Vol. 6, No. 5-6, p. 527-531, May-June (2012).
- [2]. K. A. Meradi and F.Tayeboun, Tunable Filter Based Upon Thue-Morse Photonic Crystal Structures, *Journal of Russian Laser Research*, volume 36, number 4, July, (2015).
- [3]. Fabrice Kwefeu Mbakop, Noel Djongyang and Danwe Raidandi, One Dimensional TiO_2 / SiO_2 Photonic Crystal Filter For Thermo Photovoltaic Applications, *Journal of European Optical Society, Rapid Publications*, 12:23 (2016).
- [4]. Sergey A. Dyakov, Vladimir A. Tolmachev, Ekaterina V. Astrova, Sergey G. Tikhodeev, Viktor Yu. Timoshenko, Tatiana S. Perova, Numerical Method For Calculation Of Optical Properties Of Layered Structures, *International Conference on Micro- and Nano-Electronics 2009*, edited by Kamil A. Valiev, Alexander A. Orlikovsky, *Proc. of SPIE* Vol. 7521, 75210G-1 CCC-code:0277-786X/10/\$18 doi:10.1117/12.862566 , SPIE, (2010).
- [5]. Saeed Golmohammadi, 32-Channel Optical Interleaver / Deinterleaver Using Fibonacci Quasi-Periodic Structures, *Progress in electromagnetic Research B*, vol. 55, 217-240, (2013).
- [6]. Asmar Aming and Ratchapak Chitaree, Design Of Channel Filter Based On Asymmetric One Dimensional Defective Photonic Crystal For Broadband Responses, *Proceedings of the international MultiConference of Engineering and Computer Scientists 2015* vol. II, IMECS, March 18-20, Hong Kong (2015).
- [7]. A. Bruyant, G. Lerondel, P. J. Reece, and M. Gal, All Silicon Omni Directional Mirror Based On One Dimensional Photonic Crystals, *American Institute of Physics, Applied physics letters*, vol. 82, no. 19, 12- May (2003).
- [8]. Qing Liu and Kin Seng Chiang, Member, IEEE, Fellow, OSA, Design Of Long Period Waveguide Grating Filter By Control Of Waveguide Cladding Profile, *Journal of light wave Technology*, vol.24, no. 9, September, (2006).
- [9]. N.Subrahmanyam Brij lal M.N. Avadhanulu, *S. Chand publication*. A text book of Optics, Ch. 3, Ch. 12 and Ch. 13, (2004).

- [10]. Quarda Barkat, Theoretical Investigation Of Transmission And Dispersion Properties Of One Dimensional Photonic Crystal, *Journal of Electrical and Electronic Engineering, Science Publishing Group*, 3(2), 12-18, (2015).
- [11]. Usmita Banerjee, Rajashree Khan, Avisek Maity, Barnisa Chottopadhyay, Arpan Deyasi, Sanjay Pal, Calculation For Transmittivity Of One Dimensional Photonic Crystal, *IJECCCT*, vol. 4, issue 3, May (2014).
- [12]. Arafa H. Aly, Mohamed Ismaeel, Ehab Abdel Rahman, Comparative Study Of The One Dimensional Dielectric And Metallic Photonic Crystals, *Optics and Photonic Journal, SciRes*, 2, 105-112, (2012).
- [13] Hamed Alipour Banaei, Somaye Serajmohammadi, Farhad Mehdizadeh, Mahdi Hassangholizadeh Kashtiban, Special Optical Communication Filter Based On Thue Morse Photonic Crystal Structure, *Optical Applicata*, Vol. XLVI, No. 1, (2016).
- [14] Y. Trabelsi, Y. Bouazzi, N. Benali, M. Kanzari, Narrow Stop Band Optical Filter Using One Dimensional Regular Fibonacci/Rudin Shapiro Photonic Quasi Crystals, accepted at 19 September 2015, (Opt Quant Electron 2016 48:54 DOI 10.1007/s11082-015-0295-y CROSS-MARK), *Springer Science +Business Media New York* (2015).
- [15]. Hamed Alipour Banaei, Farhad Mehdizadeh, Mahdi Hassangholizadeh Kashtiban, Important Effect Of Defect Parameters On The Characteristics Of Thue Morse Photonic Crystal Filters, *Hindawi Publishing Corporation Advances in Opto Electronics*, Volume 2013, Article ID 85 614 8 , 5 pages, Feb (2013).
- [16]. S.K. Shrivastava, S.P. Ojha, Omni Directional Reflection Bands In One Dimensional Photonic Crystal Structure Using Fullerene Films, *Progress In Electromagnetics Research, PIER* 74, 181–194, (2007).
- [17]. Andrey V. Tsarev, Peculiarity of Multi Reflector Filtering Technology, *11th international conference, APEIE – 30057*, (2012), and also available at 978-1-4673-2841-8/12/\$31.00, IEEE (2012).
- [18]. Xiaodong Lu, Shuxian Lun, Tao Zhou, Yuan Li, Chunxi Lu, Ming Zhang, Reflecting Filters Based On One Dimensional Photonic Crystal With Large Lattice Constant, supported by program for NCET (No:CET-11-1005), LNET (No: LR201002) NSFLN (No: 201102005), FSPLN(No:2011402001), Liaoning BaiQianWan Talents Program of China (No: 2012921061) and Educational commission of Liaoning province of China (No: L2012401), and 978-1-4799-0530-0/13/\$31.00, *IEEE*, (2013).
- [19]. Dishiti Gupta, Rajesh V. Nair, Optical Surface States At The Interface Between A Metal And Dielectric Nano Photonic Structure, *WRAP*, 1570213264 ,(2015).
- [20]. Bipin kumar singh, Praveen Chandra Pandey, Tunable Mirror And Multi Channel Filter Based On 1-D Exponentially Graded Photonic Crystals, (supported by Department of Science & Technology DST (INDIA) in the form of project, grant No. 100/IFD2489/2011-12, also available on IEEE, (2011-12).
- [21]. S K Srivastava, S P Ojha, A Novel Design Of Nano Layered Optical Filter Using Photonic Band Gap Materials, *AOMD - 2008*, also available on IEEE, (2008).